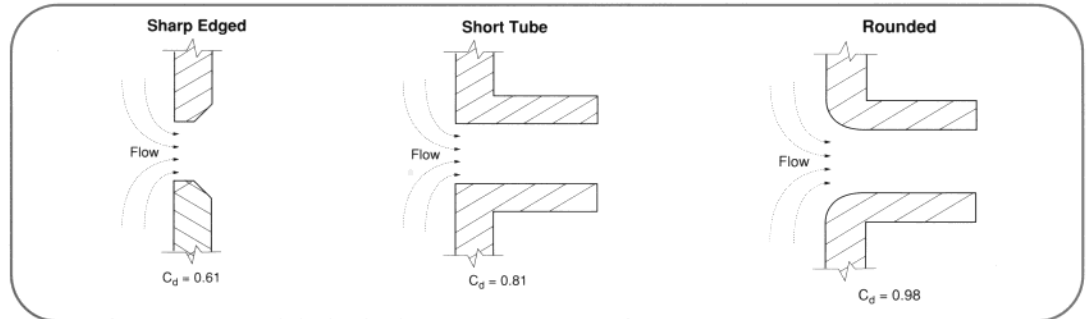


Calculating the Time Required To Empty a Vessel

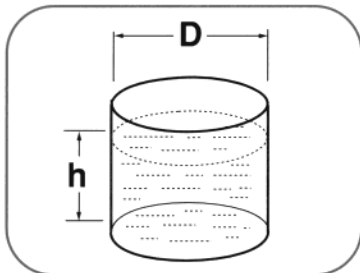
The following formulas are based on turbulent flow of a Newtonian fluid through an outlet (orifice) in a tank. The discharge coefficient C_d depends on the configuration of the outlet. Some typical values for discharge coefficient are shown at right.



Variables: h elevation of tank G gravitational acceleration = 32.2 ft/sec²
 D diameter of tank Δt time required to empty tank (sec)
 A orifice area (ft²)

Vertical Cylindrical Tank

$$\Delta t = \frac{\pi D^2}{C_d A} \sqrt{\frac{h}{8G}}$$



Example 1

A vertical cylindrical tank 12 ft in diameter is fitted with a 2" Hayward bulkhead fitting (comparable to a short tube outlet). The area of the outlet is:

$$\Delta t = \frac{\pi D_{\text{out}}^2}{4 (144)} = \frac{\pi 2^2}{4 (144)} = 0.0218 \text{ ft}^2$$

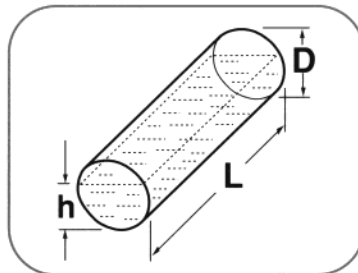
If the tank is filled with water to a height of 20 ft, and we assume turbulent flow, the approximate time to empty the tank is given by:

$$\Delta t = \frac{\pi 12^2}{0.81 (0.0218)} \sqrt{\frac{20}{8 (32.2)}} = 7,139 \text{ sec}$$

The tank should be empty in about 2 hours.

Horizontal Cylindrical Tank

$$\Delta t = \frac{L \{ D^{3/2} - (D-h)^{3/2} \}}{3 C_d A} \sqrt{\frac{8}{G}}$$



Example 2

A 7 ft diameter by 9 ft long horizontal cylindrical tank has a 4" diameter sharp edged orifice outlet. The area of the outlet is:

$$\Delta t = \frac{\pi D_{\text{out}}^2}{4 (144)} = \frac{\pi 4^2}{4 (144)} = 0.0873 \text{ ft}^2$$

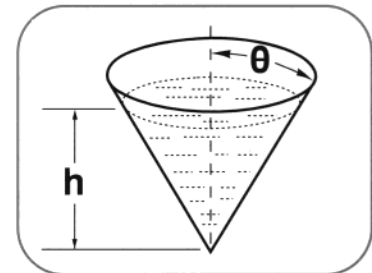
If the tank is filled with water to a height of 5 ft, and we assume turbulent flow, the approximate time to empty the tank is given by:

$$\Delta t = \frac{9 \{ 7^{3/2} - (7-5)^{3/2} \}}{3 (0.61) 0.0873} \sqrt{\frac{8}{(32.2)}} = 440 \text{ sec}$$

The tank should be empty in about 7 minutes.

Conical Tank

$$\Delta t = \frac{\pi h^{5/2} \tan^2 \theta}{5 C_d A} \sqrt{\frac{8}{G}}$$



Example 1

A conical tank with a taper angle of 25° is fitted with a 2" diameter short tube type outlet. The area of the outlet is:

$$\Delta t = \frac{\pi D_{\text{out}}^2}{4 (144)} = \frac{\pi 2^2}{4 (144)} = 0.0218 \text{ ft}^2$$

If the tank is filled with water to a height of 28 ft, and we assume turbulent flow, the approximate time to empty the tank is given by:

$$\Delta t = \frac{\pi (28^{5/2}) \tan^2 25^\circ}{5 (0.81) 0.0218} \sqrt{\frac{2}{32.2}} = 8,000 \text{ sec}$$

The tank should be empty in about 2-1/4 hours.